Earthquake Probabilities and Energy Characteristics of Seismicity Offshore Southwest Taiwan

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Received 30 November 2007, accepted 26 September 2008

ABSTRACT

We characterize fault geometries for moderate and large earthquakes in and offshore southwest (SW) Taiwan. Stress orientation estimates suggest that the first shock of the Pingtung earthquake may be characterized by slab flexure. A region of predominately normal-faulting earthquakes is also defined. Using the maximum-likelihood Gutenberg-Richter relation, we find that the repeat times for magnitude, \( M \geq 6.5 \) and \( M \geq 7.0 \) earthquakes are approximately 30 and 80 years, respectively. By assuming a Gaussian probability distribution with a standard deviation of 0.4 the recurrence time, we estimate a 50% probability of an \( M \geq 6.5 \) earthquake recurring in the next 30 years, while only a 20% probability of an \( M \geq 7.0 \) in the next 50 years. To test the empirical relation that is currently being used to convert \( M_L \) to seismic moment (\( M_0 \)), we test the well-defined energy to moment ratio (\( E/M_0 \)) for the region. We additionally utilize this method to identify the lack of slow-source earthquakes in several recent offshore events in Taiwan.

Key words: Taiwan seismicity, Gutenberg-Richter relation, Earthquake probability, Tsunami earthquake


1. INTRODUCTION

The region on land and offshore southwestern (SW) Taiwan is considered to be a zone of tectonic escape (Lacombe et al. 2001), and is identified as a zone of reduced seismic activity in Taiwan, as compared to other zones where significant collisional processes are ongoing. However, SW Taiwan is not immune to large earthquakes, as attested by the occurrence of the Pingtung earthquake on 26 December 2006. The two local magnitude (\( M_L \)) 7 offshore earthquakes (separated by approximately eight minutes) remind us, also of the potential tsunami hazards on SW Taiwan coasts where several devastating events (e.g., Anpin in 1661 and 1782) were documented (Soloviev and Go 1974). Therefore, motivated by the Pingtung earthquake, we analyzed recent activity to estimate recurrence and near future likelihood of an \( M_L \geq 7.0 \) earthquake in the SW Taiwan region. Likewise, we analyze the energy character of rupture to determine if any of these events have a slow rupture source, an indicative feature of tsunami earthquakes.

While statistical tools, such as frequency-magnitude determinations and probability analysis, are well established, we remark that the results are significantly affected by uncertainties. Hence a careful examination is necessary. Uncertainties arise because of the non-episodic nature of earthquakes, and the short total duration of sampling (e.g., Stein and Newman 2004). For the region, results suggest that the repeat time for an \( M_L \geq 7.0 \) earthquake is approximately 80 years, with a 20% probability for another \( M_L \geq 7.0 \) earthquake occurring within the next 50 years.

For improved tsunami hazard mitigation, a warning system for near-field tsunami detection is currently undertaken. The effectiveness of this system depends heavily on accurate assessment of coastal run-up heights immediately after a tsunamigenic earthquake (Wu et al. 2008). The feasibility of such a system in Taiwan hinges on the “Taiwan Rapid Earthquake Information Release System (TREIRS)” of the Central Weather Bureau (CWB), which generally reports the parameters (longitude, latitude, depth, and \( M_L \)) of an earth-

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quake within five minutes of its occurrence. One essential task is to convert the \( M_l \) scale to seismic moment (\( M_0 \)), using an empirical rule, for the calculation of approximate seafloor displacements. However, the magnitude to moment transformation may be significantly underestimated for the so-called “tsunami earthquakes” (Kanamori 1972), where the sources rupture in an exceedingly slow fashion. Here, we apply the energy-to-moment ratio discriminate of Newman and Okal (1998) for tsunami earthquake identification for past events offshore Taiwan. We find no energy deficiency that would be characteristic of tsunami earthquakes in the events analyzed. It is thus reasonable to assume that the approximate empirical conversion from the local magnitude to seismic moment is not biased by the occurrence of slow-source tsunami earthquakes.

2. METHODS

2.1 Earthquake Characterization and Tensional Rupture Orientations

The normal faulting feature of the first shock of the Pingtung earthquake suggests tensional stresses were the dominant controlling mechanism, and is consistent with seismicity associated with tectonic escape in SW Taiwan (Lacombe et al. 2001). In order to constrain the spatial extent of activity, we utilize the distribution of observed seismicity with known focal solutions. We utilized the Global Centroid Moment Tensor (gCMT) catalogue (Dziewonski et al. 1983; www.globalcmt.org), which provides global coverage of earthquake focal mechanisms of moderate and large events (moment magnitude, \( MW > 5.5 \)) since 1977. Using this catalog we constrain shallow events (depth < 70 km) within an area slightly broader than, and ultimately used to define the study region. A ternary diagram, of the type first used by Frohlich and Apperson (1992), shows the distribution of focal mechanisms within this catalog subset (Fig. 1). From this diagram, it is apparent that activity is predominantly thrust in nature, with about 2/3’s as many normal faulting events and only a few significant strike-slip events. The Pingtung earthquake is shown to consist first of a strongly normal faulting event, followed by a moderate strike-slip event.

The study region is constrained by the extent of predominant normal faulting activity (Fig. 2; further explained in section 3.2). The northeastern boundary approximately follows the Chishan Transfer Fault Zone, which separates distinctive seismic patterns to the north and south (Lacombe et al. 2001). The west and south boundaries are defined roughly according to the detected range of the CWB TREIRS.

2.2 Frequency-Magnitude Relationship

The Gutenberg and Richter (GR) law describes that the number of earthquakes (\( N \)) with magnitude larger than or equal to \( M \) follows a power law distribution (Gutenberg and Richter 1944), such that:

\[
\log_{10} N(M) = a - bM
\]

the \( b \)-value indicates the relative size and frequency of occurrence of earthquakes. Since the CWB catalogue is the source of seismicity and it reports local magnitude (\( M_l \)), we thus use \( M_l \) for the GR law analysis. The \( M_l \) of earthquakes in the CWB catalogue are routinely determined following the formula proposed by Richter (1935). The peak amplitude is measured on simulated Wood-Anderson seismograms, which are synthesized by firstly deconvolving the known instrument response and then convolving the response of the standard Wood-Anderson seismometer (natural period at 0.8 sec). An empirical law suitable for the Taiwan region is adopted for correcting the effects of hypocentral distances (Shin 1993).

We retain only shallow earthquakes (0 - 70 km) within the defined study region for the determination of the GR law relationship.

Fig. 1. Ternary diagram displaying the distribution of earthquake focal mechanisms. The three apexes indicate a pure strike-slip (top), a pure normal fault with 45° dipping plane (left), and a pure thrust fault with 45° dipping plane (right). Fractions of the three components for sampled earthquakes are indicated by their positions inside the triangle. The seismic moment of individual events are scaled by increased shading. The closer an earthquake projects to a corner, the more dominant that rupture type is. Results of the Pingtung doublet earthquakes are indicated as 1st and 2nd, respectively.
relation. Upon investigating the cumulative number of events as a function of year, we find that the slope changes from nearly flat to relatively steep by 1979, corresponding to the installation of the Taiwan Telemetered Seismographic Network between 1972 and 1987 (Wang 1989). We thus deem that the CWB catalogue is nearly complete beginning in 1979 and only the time period between 1979 and 2007 is analyzed.

The maximum-likelihood technique for calculating the $b$-value is adopted (Aki 1965; Woessner and Wiemer 2005):

$$b = \frac{\log_{10} (e)}{\langle M \rangle - \frac{M_c - \Delta M_{\text{bin}}}{2}}$$

(2)

where $e$ is approximately 2.718, $\langle M \rangle$ is the mean magnitude, $M_c$ is the minimum magnitude of completeness defined as the lowest magnitude at which 100% of the events are detected in the catalog, and $\Delta M_{\text{bin}}$ is the binning width (0.01 in this study). To determine the optimal $M_c$ of the catalog, approaches of Wiemer and Wyss (2000) are followed. Firstly, the $a$- and $b$-value as a function of minimum magnitudes ($M_c$) and an infinite maximum magnitude are determined. Secondly, residuals ($R$) for each derivation are calculated using (Wiemer and Wyss 2000):

$$R(a, b, M_c) = \frac{\sum_{i=1}^{M_{\text{max}}} |B_i - S_i|}{\sum_{i=1}^{M_{\text{max}}} B_i} \times 100$$

(3)

where $B_i$ and $S_i$ are the cumulative number of events in each magnitude bin from observation and synthetics. $M_{\text{max}}$ is the magnitude of largest earthquakes in the dataset. The optimal $M_c$ is then determined at which $R$ is minimum (Fig. 3). Furthermore, to alleviate the saturation problem of $M_c$ scale, we set $M_c = 6.0$ as the upper bound magnitude for the determination of $a$- and $b$-values.

2.3 Probability Analysis

From the derived GR law, we extrapolate to larger events at lower recurrence rates to estimate the repeat time of earthquakes with a given magnitude ($M$). Because $M_c$ begins to saturate near $M_c = 6.5$, where rupture durations significantly exceed the natural period of the Wood-Anderson seismometer it is necessary to continue with a generic magnitude characterization, $M$. This type of relationship has been shown using body-wave magnitudes (Okal and Romanowicz 1994), and its application is further described in Newman et al. (1999). We estimate the probabilities of two scenarios
within the study region: (1) an \( M \geq 6.5 \) earthquake to occur in the next 30 years, and (2) an \( M \geq 7.0 \) earthquake to occur in the next 50 years. The estimation is equivalent to calculating the conditional probability of an earthquake occurring between \( T_0 \) (the year 2007) and \( T \) (the year 2037 for an \( M \geq 6.5 \) and the year 2057 for an \( M \geq 7.0 \)). The probability density function is assumed to be a Gaussian distribution with the mean taken as the repeat time, and the standard deviation taken as 0.4 of the mean repeat time (Nishenko and Buland 1987).

2.4 The \( E/M_0 \) Discriminant for Tsunami Earthquakes

We adopted the dimensionless parameter \( \Theta = \log_{10} (E/M_0) \) as proposed by Newman and Okal (1998) to discriminate tsunami earthquake from recent large offshore earthquakes around Taiwan (not limited to the study area). A tsunami earthquake will exhibit a reduction of one or more units in \( \Theta \), representing at least a 10-fold decrease in radiated energy \( (E) \) than expected for its seismic moment \( (M_0) \). This is because tsunami earthquakes rupture more slowly, having a low corner frequency, and hence have minimal shaking for the same amount of slip. While \( M_0 \) can readily be obtained from the gCMT catalogue, we calculate the energy using the algorithm given by Boatwright and Choy (1986) and modified by Newman and Okal (1998).

Briefly, the energy algorithm calculates the energy flux of the generalized P wave group \( (P, pP, \text{ and } sP) \) recorded at teleseismic stations, which has been corrected both for instrument response and receiver function (Okal 1992). The calculated flux is then scaled back to a focal sphere, accounting for radiation pattern, geometrical spreading and frequency-dependent attenuation (Newman and Okal 1998). The radiated seismic energy is finally obtained by integrating over the unit sphere, and adding those of the generalized S wave group \( (S, pS, \text{ and } sS) \), expressed as a constant correction for the ratio of Energy in the P vs. S waves of 4/15 (Boatwright and Fletcher 1984).

3. RESULTS

3.1 Earthquake Characterization and Tensional Rupture Orientations

Figure 1 indicates that the first shock of the Pingtung earthquake is normal faulting, whereas the second shock is strike-slip faulting. We group the results of earthquakes in the gCMT catalogue into three categories (Fig. 1): normal faulting (NF), strike slip faulting (SF), and thrust faulting (TF). Of the 57 earthquakes in the catalog (excluding the Pingtung doublet), approximately 42% of activity is strongly thrust in nature, while about 26% is strongly normal faulting, and only 7% is strongly strike-slip. The rest of the seismicity is a mixture of these mechanisms, but are less dominant in orientation, yielding inferred stress orientations without a near-vertical principle component.

The orientations of tension axes from normal faulting earthquakes are examined geospatially (Fig. 2). The two on-land events in SW Taiwan show NE-SW trending tension axes, consistent with tectonic escape. However the four events in the Taiwan strait exhibit strong N-S trending axes suggesting a dominant and presumably unassociated extension. Most interestingly, almost all events south of Taiwan (including the Pingtung first shock) have predominantly E-W tension axes. These axes are near-normal to the trench, suggesting their origins is due to bending stresses in the slab.

3.2 Spatial Patterns of Different Earthquake Rupture Types and Determination of Study Area

A spatial pattern is observed that while most normal-faulting earthquakes, possibly caused by tectonic escape or slab bending, are located to the south and west of southern Taiwan, most thrust-faulting earthquakes, occurring as a result of Philippine-Eurasia collision, occur in a linear N-S trend to the east (Fig. 2). This pattern is consistent with the geological understanding of the tectonic setting of the Heng-chun Peninsula. It is the spatial pattern that enables us to define the boundary of the study region consisting of mainly normal faulting earthquakes in and to the southwest of Taiwan and extending the approximate coverage range of the CWB TREIRS (Fig. 2).

3.3 Frequency-Magnitude Analysis

Residuals as a function of minimum magnitude used show that the optimal value occurs at \( M_L = 2.8 \) (Fig. 3). We thus use earthquakes with \( 2.8 \leq M_L \leq 6.0 \) to determine the GR law for the study region. The best fitting GR relation is determined to be \( \log_{10} N = 5.92 - 0.87 M_L \) (Fig. 4). We use this result to extrapolate the recurrence times for larger \( M \) 6.5 and 7.0 at approximately 30 and 80 years, respectively. Because earthquakes larger than this size will likely have elongated rupture dimensions due to finiteness of rupture depth, great caution should be used in further extrapolation to even larger magnitudes. Any such direct extrapolation will likely underestimate recurrence times.

The results from extrapolation are roughly consistent with the yearly moment release of earthquakes for the past century within the study region (Fig. 5), where \( M \geq 7.0 \) events only occurred in 1900 and 2006. Figure 5 is produced by the conversion relation \( \log_{10} (M_D) = 1.45 M_L + 16.03 \), based on a linear fitting of common earthquakes recorded by the CWB catalogue and the gCMT catalogue within the study region.

3.4 Earthquake Probabilities

Given the 30- and 80-year repeat times, we construct the
Gaussian distribution, with 12- and 32-year standard deviation, of the probability density distribution relative to the year 2007, corresponding to the Dec. 2006 Pingtung earthquake (top Fig. 6). Upon calculations of the conditional probabilities, we estimate that the probability of an $M \geq 6.5$ earthquake to occur in the next 30 years is about 50% and the probability of an $M \geq 7.0$ earthquake to occur in the next 50 years is about 20% (bottom Fig. 6). As shown in Fig. 6, the 30- or 50-year probability will increase with the reference year.

### 3.5 The $E/M_0$ Discriminant for Tsunami Earthquakes

We analyzed available teleseismic data of the 20 Sep. 1999 Chi-Chi earthquake (out of curiosity), along with the 31 Mar. 2002 Hualein earthquake, the 10 Dec. 2003 Cheng-kung earthquake, and the first shock of the 26 Dec. 2006 Pingtung earthquake. None exhibit reduced energy radiation, having $\Theta \sim -4.5$, and hence do not exhibit features indicative of tsunami earthquakes (Fig. 7). The near constant $\Theta$ value suggests all events have similar rupture speeds and dimensions. While none of these earthquakes exhibited a tsunami-earthquake component, this does not preclude the possibility of future such events occurring in this region. This is evident in the study of Okal and Newman (2001), where other moderate and large earthquakes in the zones of previous tsunami earthquakes were analyzed, finding that no such tsunami earthquake character were present in most events.

### 4. DISCUSSION

The rupture processes of the Dec. 2006 Pingtung earthquake doublet have been inverted by various methods to understand the kinetic behavior (e.g., Huang et al. 2008; Lee et al. 2008; Yen et al. 2008). Dynamically, the orientation of tension axis of the first shock exhibits a direction roughly normal to the strike of the Manila trench, suggesting that the causing stresses may be associated with slab flexure, bending or unbending, with the latter proposed by Liao et al. (2008). In any case, it justifies the presence of the Luzon slab here, while the surface feature of the Manila trench is rather obscure.

The tensional-stress environment in the SW Taiwan on-land and offshore, as demonstrated by the spatial pattern of the gCMT focal solutions enables us to isolate seismicity of one type for statistical analysis. Although the $b$-value of normal faulting events is expected to be higher than those of thrust or strike-slip events (Schorlemmer et al. 2005), the obtained $b \sim 0.87$ is less than the universal observed constant of $b \sim 1.0$. This may represent characteristics of the study area and/or the CWB catalogue. Furthermore, although the south and west boundaries of the box to group the study area are constrained by the detectable range of the CWB catalogue, it is obvious that areas relatively far away from the main Taiwan island suffers problems of undersampling as shown by the sparse seismicity. As a result, the probability for an $M \geq 7.0$ earthquake to occur within the study area would be somewhat higher than 20%.
5. CONCLUSIONS

We observe a spatial pattern of moderate and large earthquakes with different rupture mechanisms; while earthquakes on and offshore SW Taiwan, and below the Manila accretionary wedge exhibit normal faulting, possibly caused by tectonic escape or slab bending, earthquakes to the right (on the arc) display predominantly thrust faulting, due to Philippine-Eurasia collision. The Gutenberg-Richter power-law distribution of seismicity within the tensionally-stressed area suggests that earthquakes of $M \geq 7.0$ event will recur about once every 80 years. After the 26 Dec. 2006 Pingtung doublet earthquakes, we estimate that the probability of an $M \geq 7.0$ earthquake to occur in the area within the next 50 years is about 20%. We calculated the $E/M_0$ ratio of past four Taiwanese earthquakes: the 20 Sep. 1999 Chi-Chi earthquake, the 31 Mar. 2002 Hualein earthquake, the 10 Dec. 2003 Chengkung earthquake and the 26 Dec. 2006 Pingtung earthquake (the first shock). Results suggest that none exhibit deficient energy, and hence none have features of tsunami earthquake rupture. Because the $E/M_0$ ratios for these four events are near constant, it is reasonable to assume that the approximate empirical conversion from our local magnitude to seismic moment is not biased by tsunami earthquakes. However, caution should be taken, because this does not preclude the likelihood of a tsunami earthquake occurring in this region in the future. If so, that event will yield an underestimate of the seismic moment by as much as a factor of 10 or more.

Acknowledgements We thank Central Weather Bureau in Taipei for earthquake catalogue. We thank W. H. K. Lee and E. A. Okal for improvements of the manuscript. This research was supported by the Taiwan Earthquake Research Center (TEC) funded through National Science Council (NSC) with grant number 95-2116-M-008-002. The TEC contribution number for this article is 00039.

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