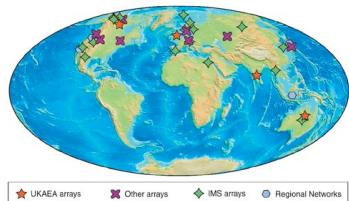


EAS 8803 - Obs Seismology

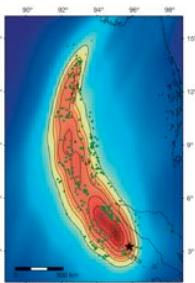
Lec#13: Array Analysis

- Dr. Zhigang Peng, Spring 2013



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Last Time

- Stacking in exploration geophysics
- Stacking to obtain reliable deep Earth structure
- Stacking to estimate seismic source properties

2

This Time

- Data management and basic data processing tools
- Systematic and random errors
- Waveform stacking
- Array analysis

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3

Array Analysis

- Introduction of array
- Basic array processing techniques
- Example of array processing techniques for Earth structures
- Example of array processing techniques for earthquake source properties

4

Definition

- **Seismic array:** many uniform seismometers in a well-defined, closely-spaced configuration (*Rost and Thomas*, Rev. Geophys., 2002).
- *Rost and Garnero* (EOS, 2004) gave the following criteria for **seismic array**:
 - Three or more seismometers
 - An aperture of more than 1 and less than a few hundred kms
 - Uniform instrumentation and recording
 - A means of analysis of the data as an ensemble
 - A common time signal.

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Definition

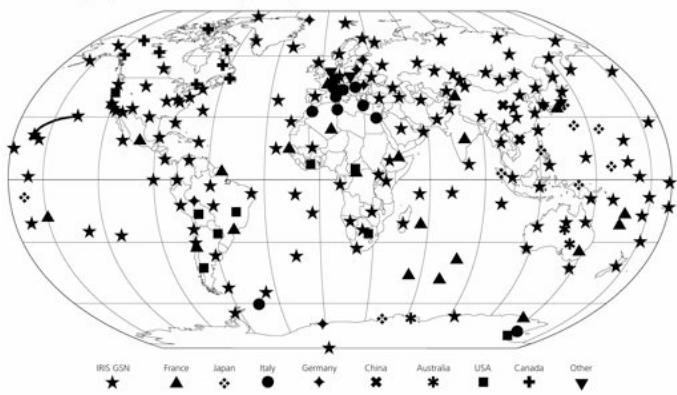
- Array processing techniques: methods of using the abilities of seismic arrays to measure the vector velocities of an incident wavefront, i.e., **slowness** and **back azimuth**.
- Difference between global and regional seismic network: more focused in the purpose, more strict in their configuration, and different analysis tools.

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Figure 6.6-16: Station map of the Federation of Digital Broad-Band Seismographic Networks (FDSN).

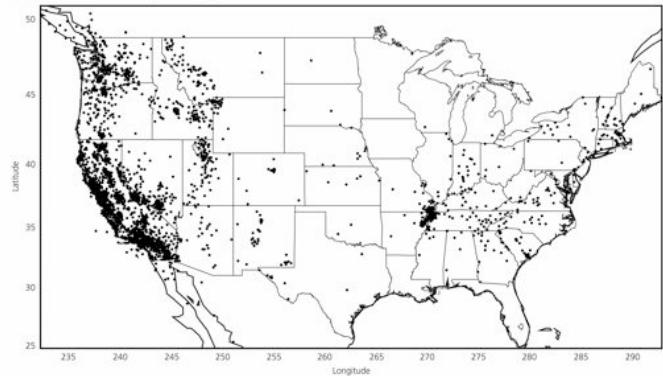


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Figure 6.6-18: Map of regional network seismometers in the continental USA.

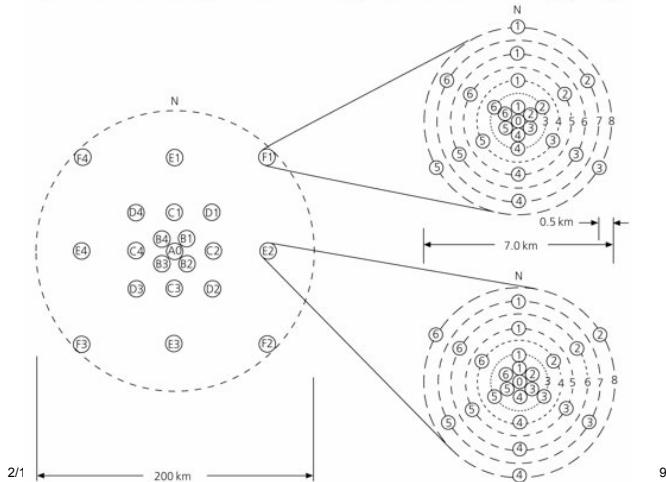


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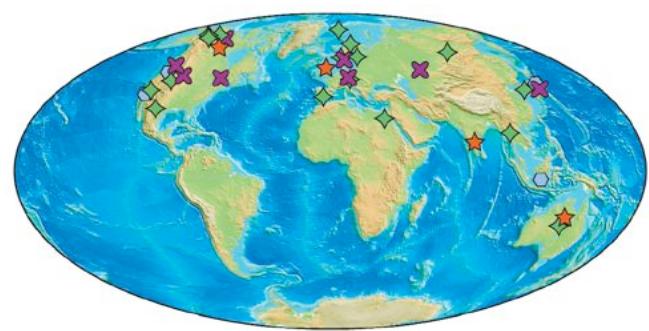
8

Figure 6.6-17: Station geometry of the Large Aperture Seismic Array (LASA).



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Why should we use arrays?

- This information can be used to **distinguish between different seismic phases**, separate waves from different seismic events and **improve the signal-to-noise ratio** by stacking with respect to the varying slowness of different phases.
- The **vector velocity information of scattered or reflected phases** can be used to determine the region of the Earth from whence the seismic energy comes and with what structures it interacted.

Why should we use arrays?

- Therefore seismic arrays are perfectly suited to study the **fine-scale structure** and **spatio-temporal variations** of the material properties of the Earth's interior.
- Array analysis can also be used to better quantify the **seismic source mechanisms** (e.g., rupture duration, velocity, areas, etc), and **forensic seismology** (Nuke detection, terrorist attacks, etc).

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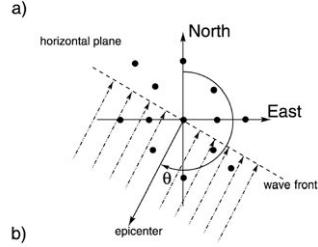
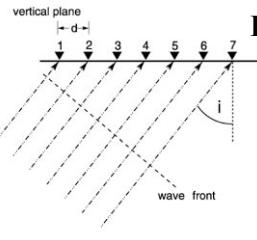
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Basics of Array Analysis (AA)

- Most array analysis methods assume a plane wave arriving at the array.
- This is a good approximation for teleseismic events.
- The propagation of an elastic waves can be described by two parameters:
 - Vertical incident angle i ,
 - Back azimuth θ .
- In practice, we often use the inverse of the apparent velocity of the wavefront $1/V_{app}$

$$u = \frac{1}{V_{app}} = \frac{\sin i}{V_0}$$

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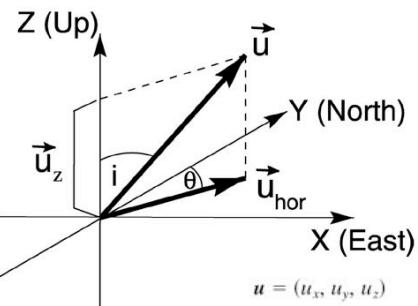


Figure 2. Components of the slowness incident angle i and back az are marked. The slowness vector is front.

$$\mathbf{u} = (u_x, u_y, u_z)$$

$$= \left(\frac{\sin \theta \cos i}{v_{app}}, \frac{1}{v_{app}}, \frac{1}{v_{app} \tan i} \right)$$

$$= u_{\text{hor}} \left(\sin \theta, \cos \theta, \frac{1}{\tan i} \right)$$

$$= \frac{1}{v_0} (\sin i \sin \theta, \sin i \cos \theta, \cos i). \quad (2)$$

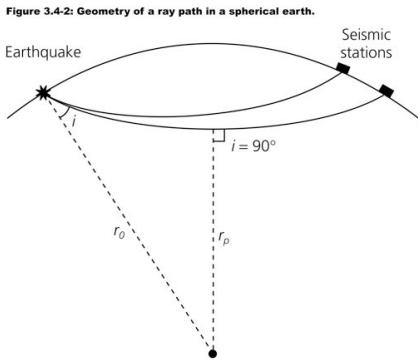
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A the surface:

$$P = \frac{r_0}{v_0 \sin i} = r_0 u$$

At the bottoming depth,
 $r = r_p$, and

$$P = \frac{r_p}{v_p}$$



The slowness \mathbf{u} is a way to identify different phases traveling through the Earth's interior as it is unique to a given phase in a one-dimensional Earth.

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Beam forming

- An important use of seismic arrays is the separation of coherent signals and noise. The basic method to separate coherent and incoherent parts of the recorded signal is **array beam forming**.
- Beam forming** uses the differential travel times of the plane wave front due to a specific slowness and back azimuth to individual array stations.
- If the single-station recordings are appropriately shifted in time for a certain back azimuth and slowness, all signals with the matching back azimuth and slowness will sum constructively.

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Station Geometry

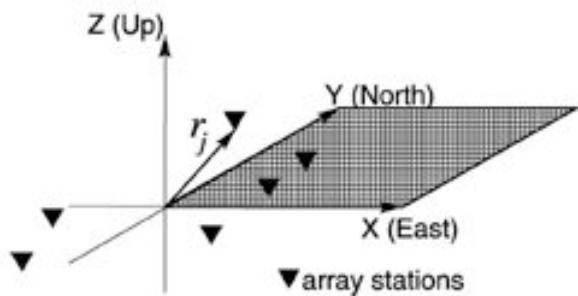


Figure 3. The definition of the sensor position vectors \mathbf{r}_j . The center of the array is assumed to be in the center of the Cartesian coordinate system.

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Delay and Sum

The incident wavefield at the array center

$$x_{\text{center}}(t) = f(t) + n_i(t).$$

Station i with the location \mathbf{r}_i records the time series:

$$x_i(t) = f(t - \mathbf{r}_i \cdot \mathbf{u}_{\text{hor}}) + n_i(t)$$

with \mathbf{r}_i representing the location vector of station i and \mathbf{u}_{hor} representing the horizontal slowness vector.

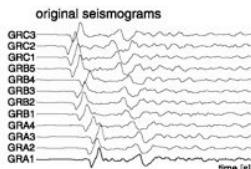
$$\tilde{x}_i(t) = x_i(t + \mathbf{r}_i \cdot \mathbf{u}_{\text{hor}}) = f(t) + n_i(t + \mathbf{r}_i \cdot \mathbf{u}_{\text{hor}}).$$

The “delay and sum” beam trace for an array with M components is then computed by

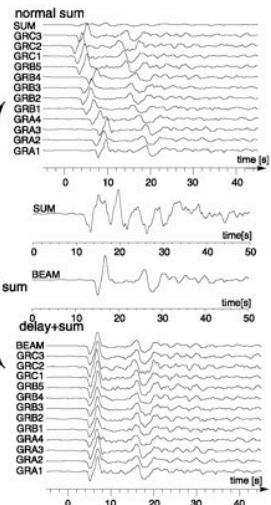
$$b(t) = \frac{1}{M} \sum_{i=1}^M \tilde{x}_i(t) = f(t) + \frac{1}{M} \sum_{i=1}^M n_i(t + \mathbf{r}_i \cdot \mathbf{u}_{\text{hor}}).$$

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Example of plain sum and “delay and sum”

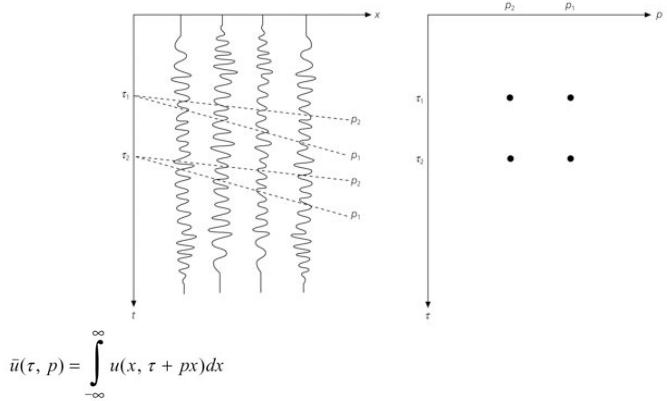


Seismic recordings of the Gräfenberg array (GRF) of an event in the Lake Tanganyika region (Tanzania/Burundi).



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Figure 3.3-23: Illustration of slant stacking.



This integral (slant stack) maps all the data along each slanted line in (x, t) to a point in (τ, p) .

20

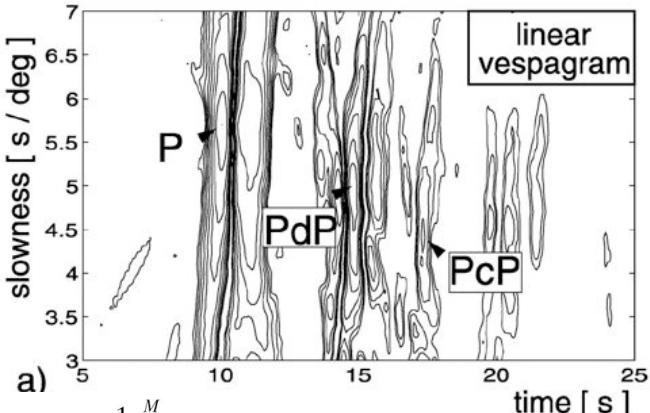
Vespa Process–Slant Stacks

- The **beam forming method** enhances the amplitude of a signal with a given slowness u .
- To determine the unknown horizontal slowness or the back azimuth of an arriving signal, the so-called **vespa process** (velocity spectral analysis [Davies et al., 1971]) can be used.
- The **vespa** in its original form [Davies et al., 1971] estimates the seismic energy arriving at the array for a given back azimuth and different horizontal slownesses u .
- Alternatively, the **vespa process** can be used for a fixed slowness and varying back azimuths.
- The result of the **vespa process** is displayed as a **vespagram**, a diagram of the energy content (amplitudes) of the incoming signals as a function of slowness or back azimuth and time.

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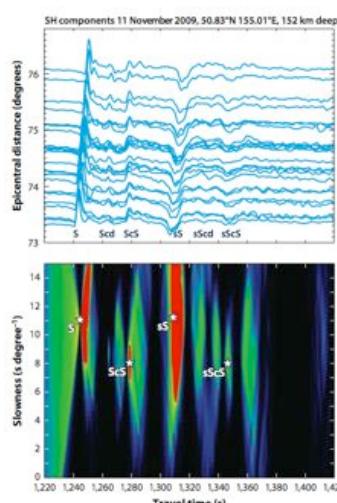
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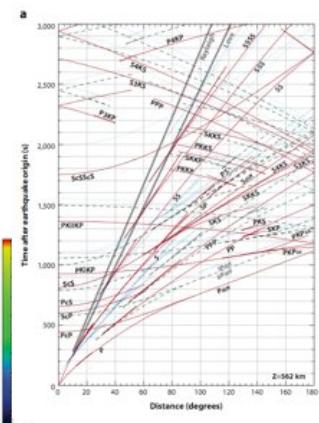


$$v_u(t) = \frac{1}{M} \sum_{i=1}^M x_i(t - t_{u,i}), \quad g = \frac{\pi 6371 \text{ km}}{180^\circ} \approx 111.91 \text{ km/}^\circ.$$

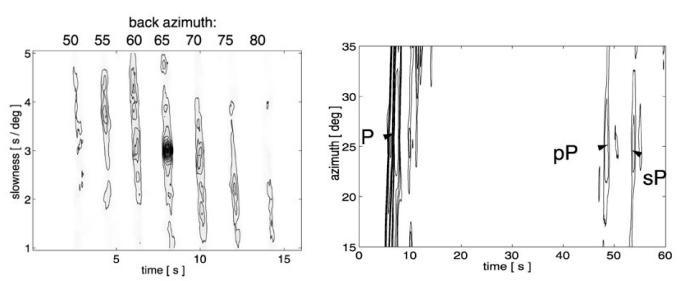
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Lay and Garnero (AREPS, 2011) 23



A wrong back azimuth (slowness) used for the computation may produce misleading slowness (back azimuth) measurements.



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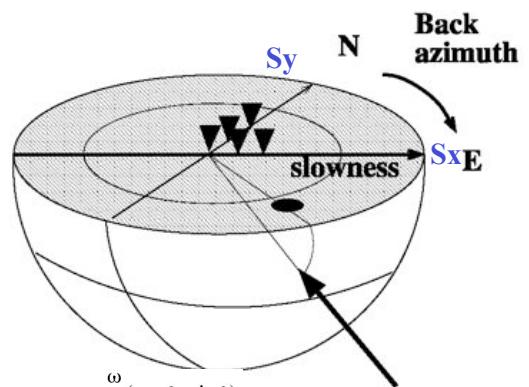
Frequency-wave number analysis

- In contrast to the array methods previously introduced, the **frequency-wave number analysis** (**fk analysis**) can measure the complete slowness vector (i.e., back azimuth θ and horizontal slowness u) simultaneously.
- A **grid search** for all u and θ combinations can be performed to find the best parameter combination, producing the highest amplitudes of the summed signal.

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$$\mathbf{k} = (k_x, k_y) = \omega \cdot \mathbf{u} = \frac{\omega}{v_0} (\cos\theta, \sin\theta)$$

$$v_{app} = 1/u_{hor} = \frac{1}{\sqrt{s_x^2 + s_y^2}}$$

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$$\theta = \tan^{-1}\left(\frac{s_x}{s_y}\right)$$

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Three-component Array Processing Techniques

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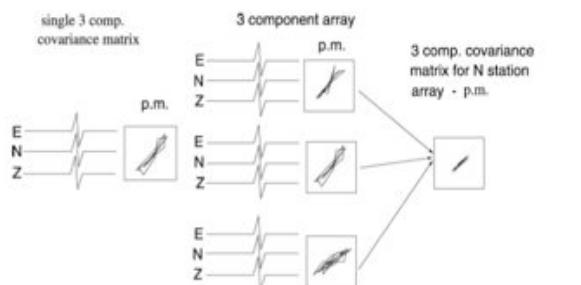


Figure 18. The principle using a three-component array for particle motion studies. For a single three-component station the covariance matrix describes the characteristics of the particle motion. For an array of three-component stations the mean of the covariance matrices of all stations is calculated. The resulting particle motion shows a smaller variance than the individual stations, and the characteristics of the motion as described in the text can be determined with smaller errors.

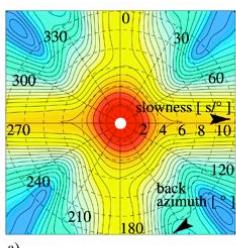
Array design principle

- Depending on the application of the array (detection, frequency of interest), their geometries vary significantly.
- Design principle:**
 - The ARF should have a **sharp main lobe**, ideally a delta pulse with a strong suppression of the energy next to the main lobe.
 - The **sidelobes** due to spatial aliasing should not be within the wave number window of interest.
 - The **aperture** of the array affects the sharpness of the main lobe, i.e., the resolution of the array.
 - The **interstation spacing** defines the position of the sidelobes in the ARF and the largest resolvable wave number; that is, the smaller the interstation spacing, the larger the wavelength of a resolvable seismic phase will be.

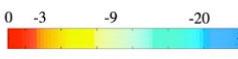
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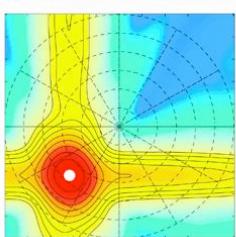
28



Array response function (ARF)
of the small-aperture Yellowknife
array (YKA) in northern
Canada.



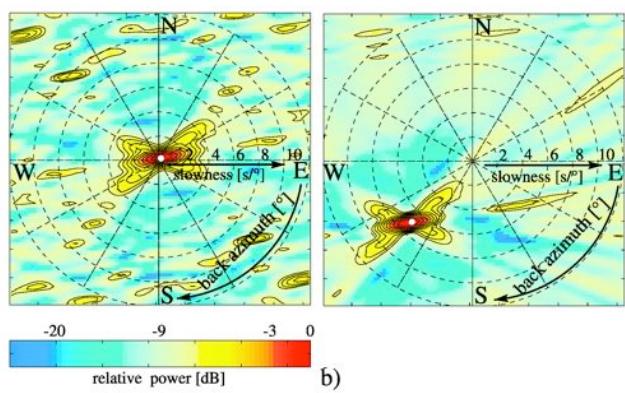
b)



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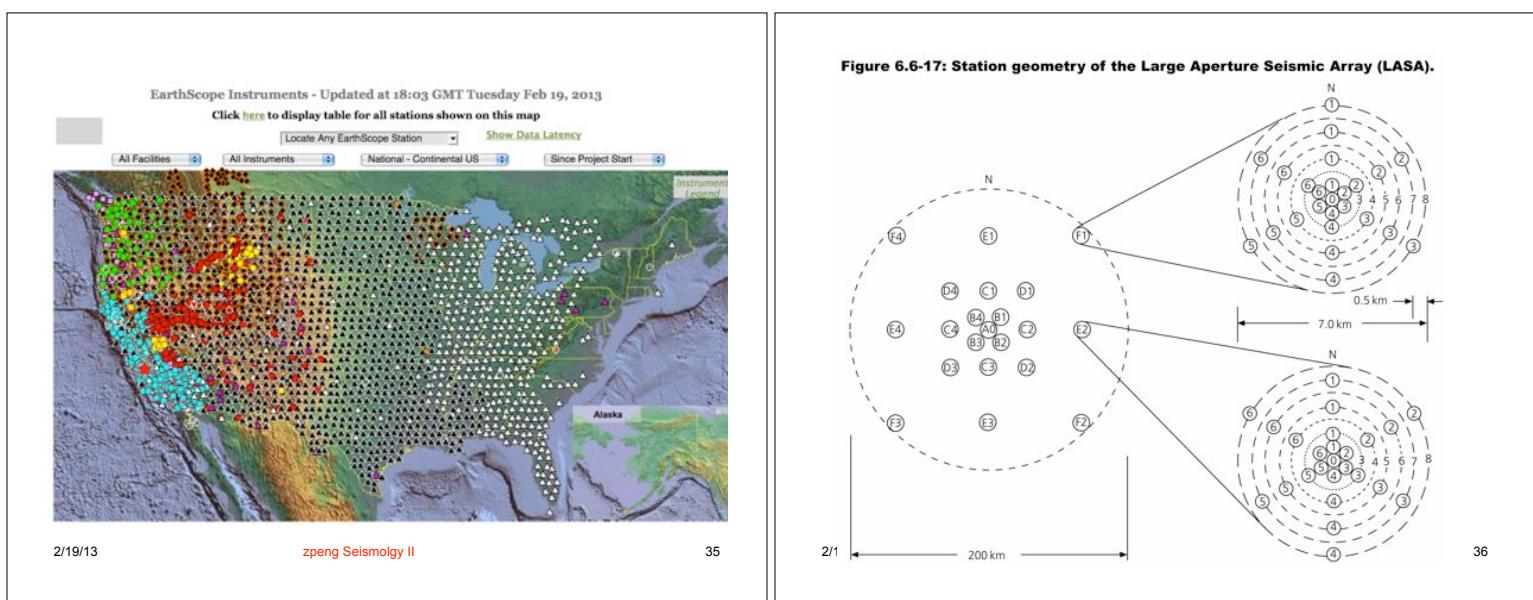
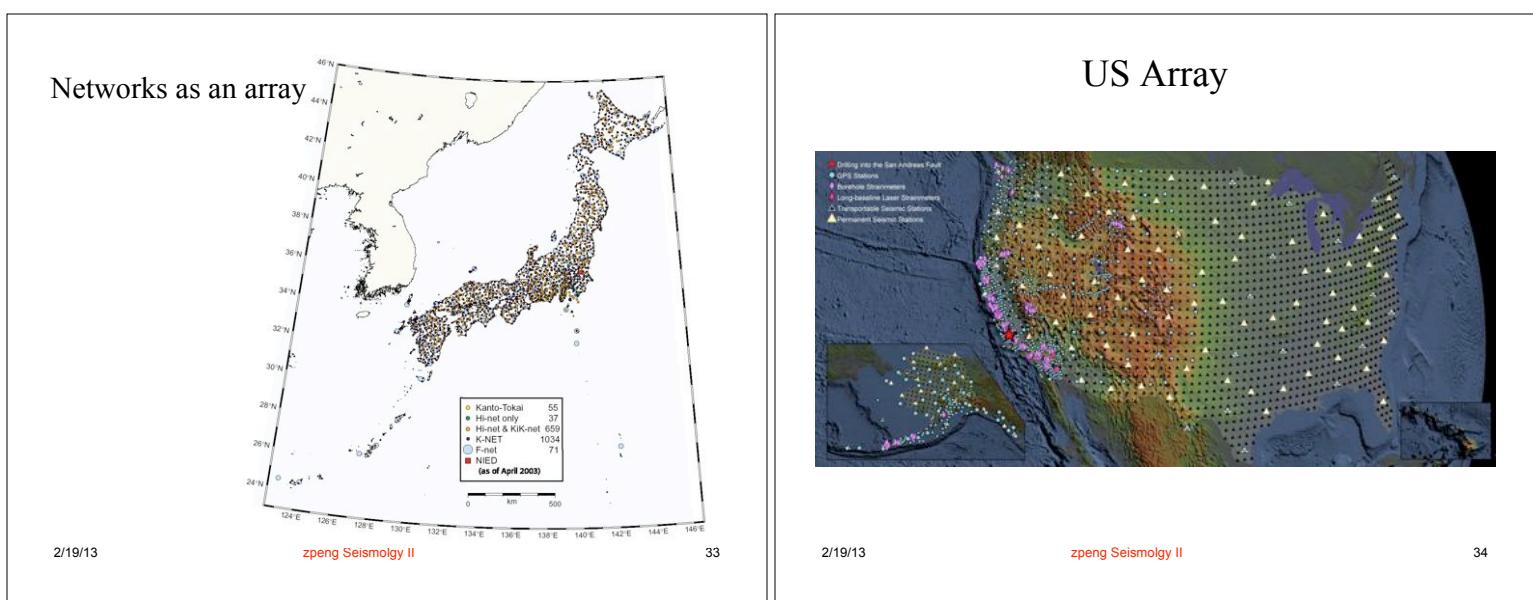
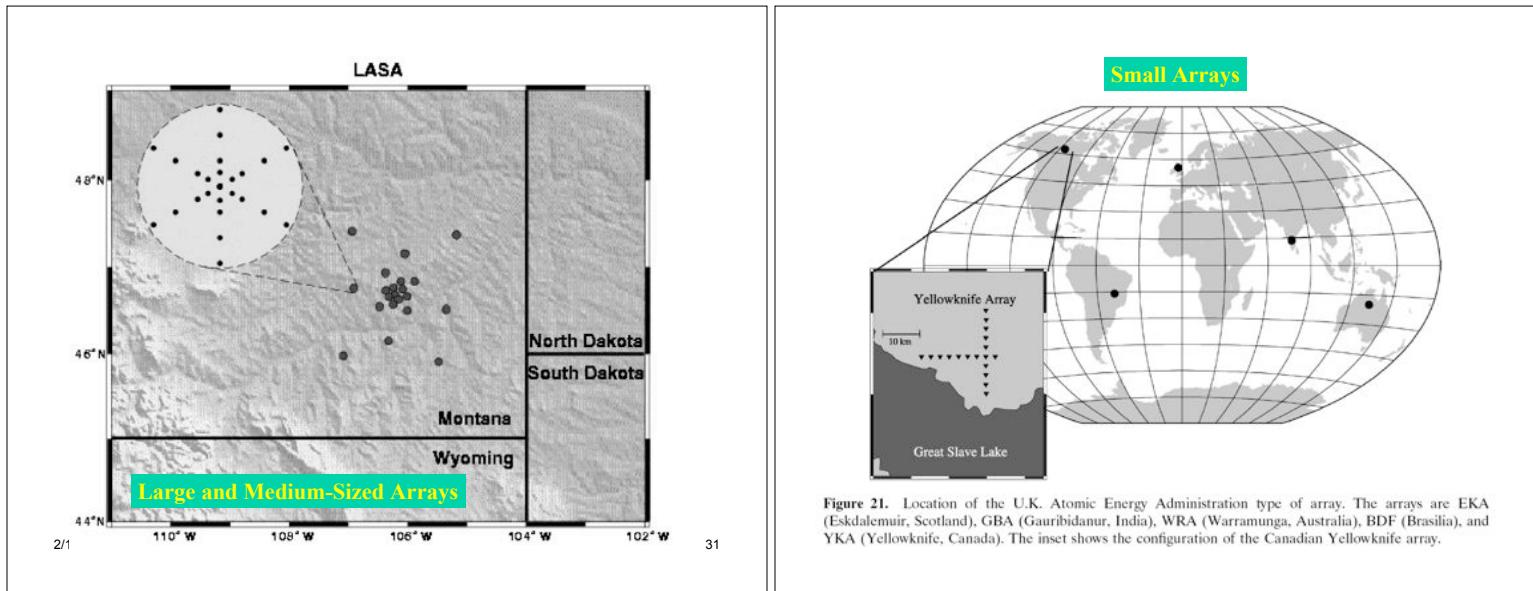
Array response function of GRF.

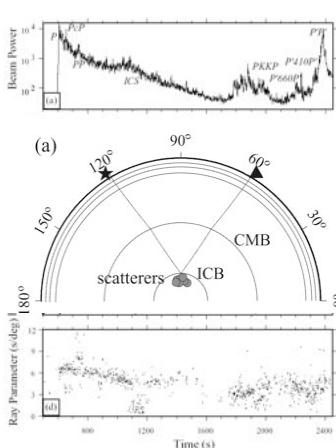


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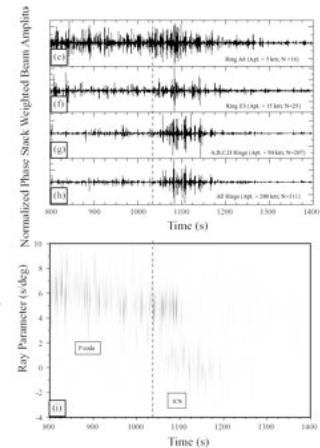




Peng et al. (JGR, 2008)
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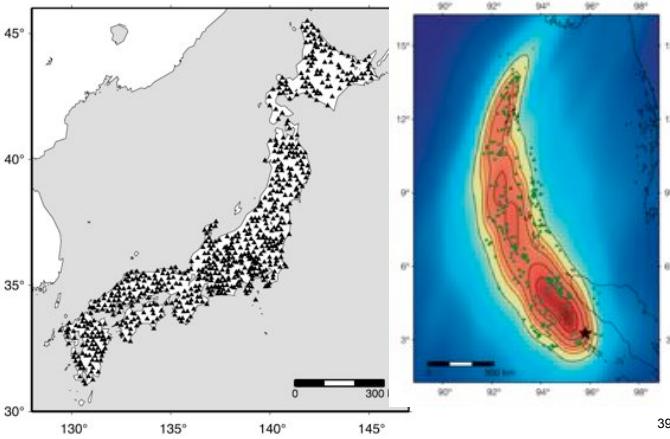
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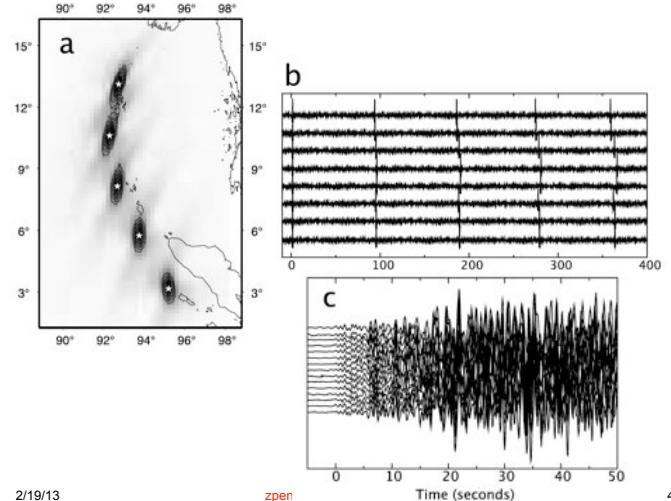
Vidale et al., Nature (2000)

38

Backpropagation imaging of the 2004 Sumatra earthquake (Ishii et al., Nature, 2005)



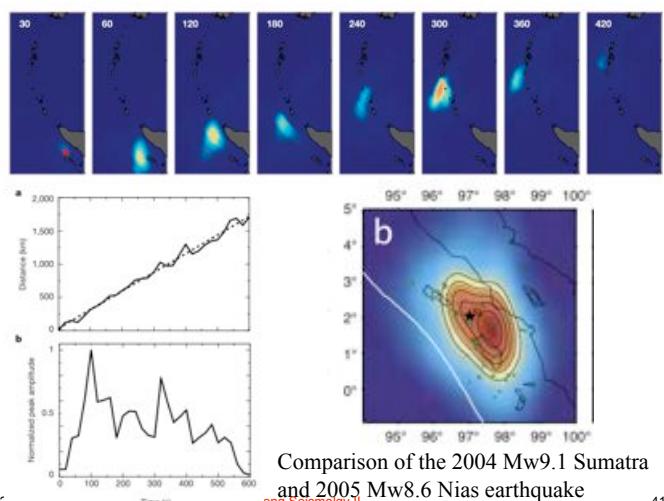
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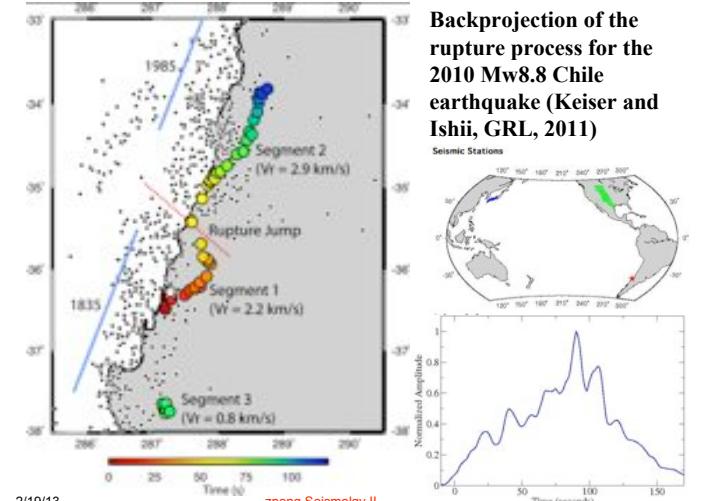
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Comparison of the 2004 Mw9.1 Sumatra and 2005 Mw8.6 Nias earthquake
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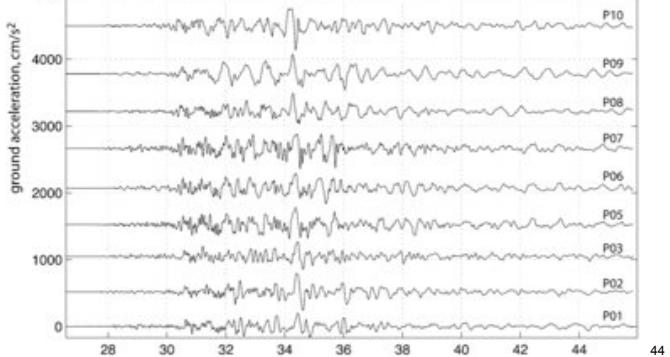
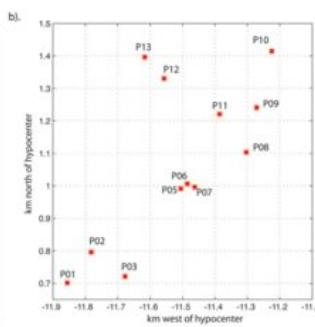
USGS Parkfield Dense Seismic Array (UPSTAR) near the Parkfield section of the San Andreas Fault in Central California (Fletcher et al., BSSA, 2006)



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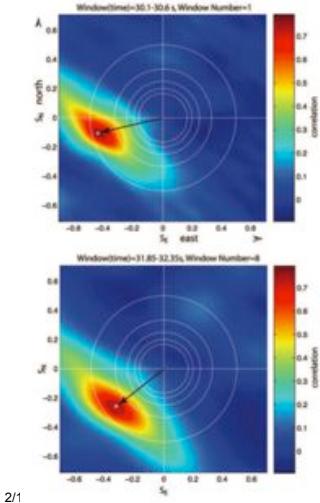
43



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How to do array processing by yourself

1. Write your own matlab script (part of homework 3).
2. Use an existing software package called **GAP (Generic Array Processing)** written by Prof. Keith Koper (SLU, now at Univ. Utah)
3. Source code and example
http://geophysics.eas.gatech.edu/people/zpeng/Software/GAP_koper_linux_all.tar.gz
4. Manual
http://geophysics.eas.gatech.edu/people/zpeng/Software/GAP_manual.pdf



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This Time

- Data management and basic data processing tools
- Systematic and random errors
- Waveform stacking
- Array analysis

• Further reading lists:

- Rost, S., and C. Thomas (2002), Array seismology: Methods and applications, Rev. Geophys., 40(3), 1008, doi:10.1029/2000RG000100.
- http://geophysics.eas.gatech.edu/internal/papers/2002/Rost_Thomas_RG_2002.pdf
- S. Rost and E.J. Garnero (2004), Array seismology advances Earth interior research, EOS, 85, 301, 305-306.
- http://geophysics.eas.gatech.edu/internal/papers/2004/Rost_Garnero_EOS_2004.pdf

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