EAS 8803 - Seismology II Lec#1: Introduction, Fourier Series Dr. Zhigang Peng, Spring 2008

Today's Outline

- Course Introduction
 - Class logistics, requirements and policies
 - Class schedule
- Introduction to digital signal processing and its relation to seismological research
- · Fourier series

Reading: Stein and Wysession Chap. 6.1 – 6.2

Time and Place

• Lecture Time: M,W 10:05 am - 11:25 am

• Lecture Place: ES & T, 1229

• My office hour: M,W 11:25 am - 12:25 pm

Class website:

http://geophysics.eas.gatech.edu/people/zpeng/Teaching/EAS8803_S08/

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Course Goals

- This is an advanced graduate-level course designed to involve students into seismological research.
- The topics covered include digital signal processing, seismometers and seismic networks, basic and advanced seismic data processing tools, travel time and synthetic seismogram calculations, and modern topics in observational and computational seismology.

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Expected class manners

- · Classroom attendance is very important
- · Ask me if something is not clear
 - You and your classmates will learn better
- Respect your classmates
 - Don't chat, rustle newspapers, use cell phones, etc. during lecture
 - If you must leave early, try to sit near the door
 - Arrive on time!!

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Grading

- 4 homework (40%)
- 3 weeks of paper reading and discussion (30%)
- Term paper project (30%)

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Course outline – 1st half

- Digital Signal Processing
 - 1. Fourier analysis
 - 2. Linear systems
 - 3. Discrete time series and transforms
 - Seismometers, Seismic Networks, and Data Centers
 - 1. Historical development and the Earth's background noise
 - 2. The damped harmonic oscillator
 - 3. Basic types of seismic sensors and digital recording devices
 - 4. Global and regional seismic networks and data management
 - 5. Instrument response
- · Observational Seismology
 - 1. Basic data processing tools
 - 2. Data management
 - Waveform stacking
 - 4. Array analysis

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Course outline - 2nd half

Theoretical and Computational Seismology

- 1. Seismic source and representation theorems
- 2. Ray theory and travel time calculation
- 3. Theoretical seismogram calculation
- 4. Earthquake location and tomography
- Scattering

Current topics in observational and computational seismology

- 1. Spectral-element methods (SEM) and full-waveform tomography
- 2. Ambient noise tomography and seismic interferometry
- 3. Waveform back projection for imaging earthquake ruptures

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Text Book

GLOBAL SEISMOLOGY MODER GLOBAL SEISMOLOGY

Required:

S. Stein and M. Wysession, An Introduction to Seismology, Earthquakes, and Earth Structure Blackwell Publishing.

Recommended:

- K. Aki and P.G. Richards, Quantitative Seismol W.H. Freeman and Co.
- T. Lay and T.C. Wallace, Modern Global Seismology, Academic Press.

Additional material will be either handed out in class or made available on the course website.

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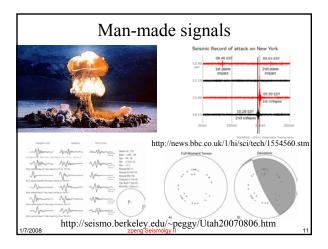
Why seismology is interesting?

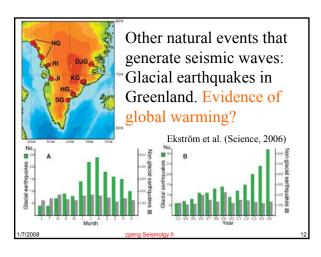
- Seismology (wikipedia): is the scientific study of earthquakes and the movement of waves through the Earth.
- Earthquakes, and other earth movements, produce different types of seismic waves.
- These waves travel through rock, and provide an effective way to "see" events and structures deep in the Earth.
- What are other types of events (not earthquakes) generating seismic signals?



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Signal and Noise

- What is the definition of signal and noise?
- •"We shall introduce the concepts of signal and noise. We define the signal as the desired part of the data and the noise as the unwanted part".
- •"Our definition of signal and noise is subjective in the sense that a given part of the data is "signal" for those who know how to analyze and interpret the data, but it is "noise" for those who do not".

Aki and Richards, Quantitative Seismology, 1980

Signal and Noise

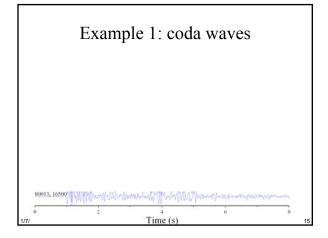


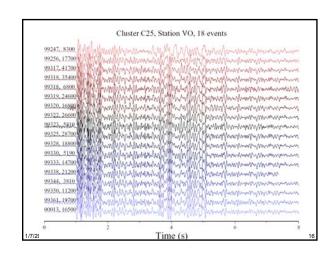
- "For example, for many years the times of the first arrivals of P- and S-waves were the only signals conveyed by an earthquake, and the rest of the seismograms, such as surface waves and coda waves, had to be considered as useless until appropriate methods of interpretations were found.
- Thus, through the application of a new technique to old data, an analyst (seismologists) can experience a moment of discovery as joyful as a data gather does using a new observational device."

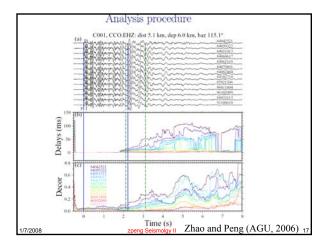
Can you think of any examples of noise turning into signal in the field of seismology?

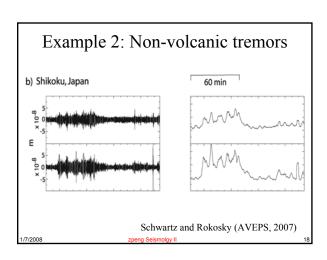


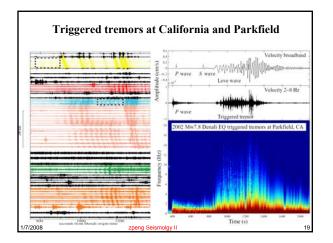
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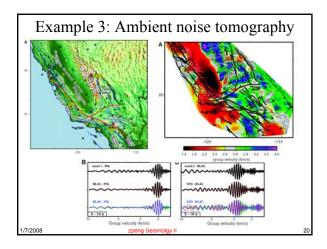


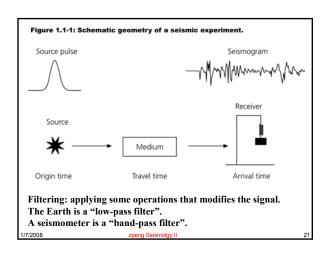












Relation between seismology and signal processing

- Seismology uses various techniques to study the displacement (or velocity, acceleration) as a function of position and time associated with elastic waves, and to draw conclusions about the seismic sources and the earth.
- A major task is seismology is to separate the source, path and site effects in order to study each of them in details.

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Relation between seismology and signal processing

- Signal processing (or time series analysis) considers functions of space or time in general terms with regard to the specific physics involved.
- Hence, many wave propagation subjects, including seismology, radar, sonar, and optics, can be treated in similar ways via signal processing technique.

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Fourier analysis

- Any time series can be decomposed into the sum or integral of harmonic waves of different frequencies.
- Harmonic waves: a sinusoid with a single frequency.

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Fourier Series

• Decomposition of a signal with a finite duration

$$f(t) = a_0 + \sum_{n=1}^{\infty} a_n \cos\left(\frac{2n\pi t}{T}\right) + \sum_{n=1}^{\infty} b_n \sin\left(\frac{2n\pi t}{T}\right)$$

• The sine and cosine Fourier terms are a set of orthogonal functions.

Fourier Series

• To find the coefficients a, and b,:

$$\int_{-T/2}^{T/2} \cos\left(\frac{2k\pi t}{T}\right) f(t) dt = \int_{-T/2}^{T/2} \cos\left(\frac{2k\pi t}{T}\right) \left[a_0 + \sum_{n=1}^{\infty} a_n \cos\left(\frac{2n\pi t}{T}\right) + \sum_{n=1}^{\infty} b_n \sin\left(\frac{2n\pi t}{T}\right)\right] dt$$

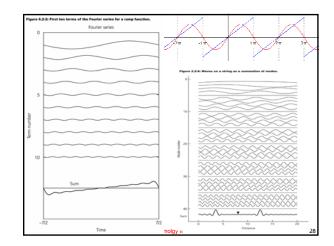
• The only nonzero term is $\cos(2\pi kt/T)$, so

$$\int_{-T/2}^{T/2} \cos\left(\frac{2k\pi t}{T}\right) f(t) dt = \int_{-T/2}^{T/2} \cos^2\left(\frac{2k\pi t}{T}\right) dt = \frac{T}{2} a_k (1 + \delta_{k0}),$$

$$a_k = \frac{2 - \delta_{k0}}{T} \int_{-T/2}^{T/2} \cos\left(\frac{2k\pi t}{T}\right) f(t) dt \qquad a_0 = \frac{1}{T} \int_{-T/2}^{T/2} f(t) dt$$

$$b_k = \frac{2}{T} \int_{-T/2}^{T/2} \sin\left(\frac{2k\pi t}{T}\right) f(t) dt$$

Simple Fourier series f(x) = x, for $-\pi < x < \pi$ $f(x+2\pi) = f(x)$, for $-\infty < x < \infty$ $\begin{aligned} a_n &= \frac{1}{\pi} \int_{-\pi}^{\pi} f(x) \cos(nx) \, dx & b_n &= \frac{1}{\pi} \int_{-\pi}^{\pi} f(x) \sin(nx) \, dx \\ &= \frac{1}{\pi} \int_{-\pi}^{\pi} x \cos(nx) \, dx & = \frac{1}{\pi} \int_{-\pi}^{\pi} x \sin(nx) \, dx \\ &= 0. & = \frac{2}{\pi} \int_{0}^{\pi} x \sin(nx) \, dx \\ f(x) &= \frac{a_0}{2} + \sum_{n=1}^{\infty} [a_n \cos(nx) + b_n \sin(nx)] & = \frac{2}{\pi} \left(\left[-\frac{x \cos(nx)}{n} \right]_{0}^{\pi} + \frac{1}{n} \right] \\ &= 2 \sum_{n=1}^{\infty} \frac{(-1)^{n+1}}{n} \sin(nx), & \text{for } -\infty < x < \infty. \end{aligned}$ http://en.wikipedia.org/wiki/Fourier_series



Complex Fourier Series

• The Fourier series can be written in a simpler form by expanding the sine and cosine functions into complex exponentials, where $\omega_n = 2n\pi/T$

$$f(t) = a_0 + \frac{1}{2} \sum_{n=1}^{\infty} [(a_n - ib_n)e^{i\sigma_n t} + (a_n + ib_n)e^{-i\sigma_n t}]$$

$$(a_n - ib_n)/2 = \frac{1}{T} \int_{-T/2}^{T/2} [\cos \sigma_n t - i\sin \sigma_n t] f(t) dt = \frac{1}{T} \int_{-T/2}^{T/2} e^{-i\sigma_n t} f(t) dt$$

$$(a_n + ib_n)/2 = \frac{1}{T} \int_{-T/2}^{T/2} [\cos \sigma_n t + i\sin \sigma_n t] f(t) dt = \frac{1}{T} \int_{-T/2}^{T/2} e^{i\sigma_n t} f(t) dt$$

· Next, we define

$$F_n = (a_n - ib_n)/2, F_0 = a_0, F_{-n} = (a_n + ib_n)/2$$
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Complex Fourier Series

· So that the Fourier series becomes

$$f(t) = F_0 + \sum_{n=0}^{\infty} [F_n e^{iw_n t} + F_{-n} e^{-iw_n t}]$$

· The negative exponentials can be written as

$$\sum_{n=1}^{\infty} F_{-n} e^{-iw_n t} = \sum_{n=-1}^{-\infty} F_n e^{iw_n t}$$

• So the Fourier series can be written in complex number

$$f(t) = \sum_{n=-\infty}^{\infty} F_n e^{iw_n t} \qquad F_n = \frac{1}{T} \int_{-T/2}^{T/2} e^{-i\sigma_n t} f(t) dt$$

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Next time

Fourier transforms

Reading: Stein and Wysession Chap. 6.1 – 6.2

"I cannot help feeling that seismology will stay in the place at the center of solid earth science for many, many

years to come...

The joy of being a seismologist comes to you, when you find something new about the earth's interior from the observation of seismic waves obtained on the surface, and realize that you did it without penetrating the earth or touching or examining it directly."



Keiiti Aki, presidential address to the Seismological Society of America, 1980

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